

This Page Is Inserted by IFW Operations
and is not a part of the Official Record

BEST AVAILABLE IMAGES

Defective images within this document are accurate representations of the original documents submitted by the applicant.

Defects in the images may include (but are not limited to):

- BLACK BORDERS
- TEXT CUT OFF AT TOP, BOTTOM OR SIDES
- FADED TEXT
- ILLEGIBLE TEXT
- SKEWED/SLANTED IMAGES
- COLORED PHOTOS
- BLACK OR VERY BLACK AND WHITE DARK PHOTOS
- GRAY SCALE DOCUMENTS

IMAGES ARE BEST AVAILABLE COPY.

**As rescanning documents *will not* correct images,
please do not report the images to the
Image Problem Mailbox.**

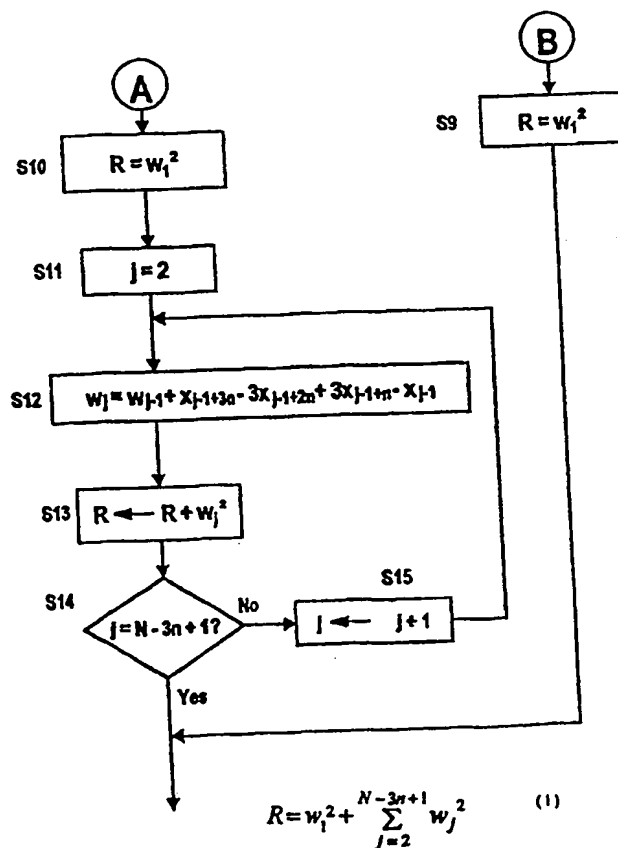


INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

(51) International Patent Classification ⁶ : G06F 17/18	A1	(11) International Publication Number: WO 99/63451 (43) International Publication Date: 9 December 1999 (09.12.99)
(21) International Application Number: PCT/EP99/03854 (22) International Filing Date: 2 June 1999 (02.06.99) (30) Priority Data: 198 25 070.3 4 June 1998 (04.06.98) DE (71) Applicant: TELEFONAKTIEBOLAGET LM ERICSSON (publ) [SE/SE]; S-126 25 Stockholm (SE). (72) Inventor: NEIHOFF, Björn; Stavsjövägen 33, S-125 41 Älvsjö (SE). (74) Agents: FÜCHSLE, Klaus et al.; Hoffmann . Eitle, Arabellas- trasse 4, D-81925 München (DE).		(81) Designated States: AE, AL, AM, AT, AU, AZ, BA, BB, BG, BR, BY, CA, CH, CN, CU, CZ, DE, DK, EE, ES, FI, GB, GD, GE, GH, GM, HR, HU, ID, IL, IN, IS, JP, KE, KG, KP, KR, KZ, LC, LK, LR, LS, LT, LU, LV, MD, MG, MK, MN, MW, MX, NO, NZ, PL, PT, RO, RU, SD, SE, SG, SI, SK, SL, TJ, TM, TR, TT, UA, UG, UZ, VN, YU, ZA, ZW, ARIPO patent (GH, GM, KE, LS, MW, SD, SL, SZ, UG, ZW), Eurasian patent (AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European patent (AT, BE, CH, CY, DE, DK, ES, FI, FR, GB, GR, IE, IT, LU, MC, NL, PT, SE), OAPI patent (BF, BJ, CF, CG, CI, CM, GA, GN, GW, ML, MR, NE, SN, TD, TG). Published <i>With international search report.</i> <i>Before the expiration of the time limit for amending the claims and to be republished in the event of the receipt of amendments.</i>

(54) Title: METHOD FOR CALCULATING THE VARIANCE**(57) Abstract**

This application describes a method and device for measuring a variation value, where a value representative of a variation between a quantity Q and a reference quantity Q_{ref} is determined by calculating error samples x_i and then determining the value R representative of the variation from (6) where each value of w_j is recursively determined from the previous value w_{j-1} . Through this recursive determination, a nested loop is avoided, whereby the amount of necessary calculation is greatly reduced.



FOR THE PURPOSES OF INFORMATION ONLY

Codes used to identify States party to the PCT on the front pages of pamphlets publishing international applications under the PCT.

AL	Albania	ES	Spain	LS	Lesotho	SI	Slovenia
AM	Armenia	FI	Finland	LT	Lithuania	SK	Slovakia
AT	Austria	FR	France	LU	Luxembourg	SN	Senegal
AU	Australia	GA	Gabon	LV	Latvia	SZ	Swaziland
AZ	Azerbaijan	GB	United Kingdom	MC	Monaco	TD	Chad
BA	Bosnia and Herzegovina	GE	Georgia	MD	Republic of Moldova	TG	Togo
BB	Barbados	GH	Ghana	MG	Madagascar	TJ	Tajikistan
BE	Belgium	GN	Guinea	MK	The former Yugoslav Republic of Macedonia	TM	Turkmenistan
BF	Burkina Faso	GR	Greece			TR	Turkey
BG	Bulgaria	HU	Hungary	ML	Mali	TT	Trinidad and Tobago
BJ	Benin	IE	Ireland	MN	Mongolia	UA	Ukraine
BR	Brazil	IL	Israel	MR	Mauritania	UG	Uganda
BY	Belarus	IS	Iceland	MW	Malawi	US	United States of America
CA	Canada	IT	Italy	MX	Mexico	UZ	Uzbekistan
CF	Central African Republic	JP	Japan	NE	Niger	VN	Viet Nam
CG	Congo	KE	Kenya	NL	Netherlands	YU	Yugoslavia
CH	Switzerland	KG	Kyrgyzstan	NO	Norway	ZW	Zimbabwe
CI	Côte d'Ivoire	KP	Democratic People's Republic of Korea	NZ	New Zealand		
CM	Cameroon			PL	Poland		
CN	China	KR	Republic of Korea	PT	Portugal		
CU	Cuba	KZ	Kazakhstan	RO	Romania		
CZ	Czech Republic	LC	Saint Lucia	RU	Russian Federation		
DE	Germany	LI	Liechtenstein	SD	Sudan		
DK	Denmark	LK	Sri Lanka	SE	Sweden		
EE	Estonia	LR	Liberia	SG	Singapore		

5

METHOD FOR CALCULATING THE VARIANCE

10 [Field of the invention]

The field of the invention relates to a method and device for measuring a value that characterizes a variation between a quantity and a reference quantity, where said
 15 variation is measured with respect to a parameter on which both the quantity and reference quantity depend. An example of this is the determination of a variation between a signal and a reference signal, both of which depend on time.

20

[Background of the invention]

A well known measure of variation is the variance which is defined as the mean value of the square of the difference
 25 between a sample value and the mean value of the samples. The standard deviation is the square root of the variance.

Specifically in connection with the characterization of timing signals, a measure of the time variation as a
 30 function of integration time is known, which is referred to as TDEV (time deviation) and is e.g. defined in ETSI European Telecommunication Standard ETS 300462-1, April 1997 or ITU-T Recommendation G.810, Series G: Transmission Systems and Media, August 1996. A time deviation TDEV is
 35 defined as

$$\text{TDEV}(n\tau_0) = \sqrt{\frac{1}{6n^2} \left\langle \left[\sum_{i=1}^n (x_{i+2n} - 2x_{i+n} + x_i) \right]^2 \right\rangle} \quad (1)$$

5

where the angle brackets denote an ensemble average, and x_i ,

with $i = 1, 2, \dots, N$, are sample values of a time error function $x(t)$ and these samples are taken at equidistant
 10 time intervals. The time dependent error function $x(t)$ is defined as the difference between a clock generating time $T(t)$ and a reference clock generating time $T_{ref}(t)$. Here, t is therefore to be understood as the absolute (abstract) time, whereas T is a signal generated by a clock that
 15 depends on t and itself also represents a time. The N sample values are sampled at equal intervals τ_0 , such that $x_i = x(i \cdot \tau_0)$, $i = 1, 2, \dots, N$. τ_0 is the sampling period and $\tau = n \cdot \tau_0$ is the observation interval.

20 The ensemble average relates to the observation interval in the sense that an average is taken over possible triplets x_{i+2n} , x_{i+n} , x_i .

The above mentioned documents contain an estimator formula
 25 for TDEV, which is:

$$TDEV(n\tau_0) = \sqrt{\frac{1}{6n^2} \frac{1}{(N-3n+1)} \sum_{j=1}^{N-3n+1} \left[\sum_{i=j}^{n+j-1} (x_{i+2n} - 2x_{i+n} + x_i) \right]^2} \quad (2)$$

30 where $n = 1, 2, \dots$ the integer part of $N/3$.

[Problem underlying the invention]

5 The problem with the above estimator formula is that a calculation results in two nested FOR-loops for the summation under the square root, and in three nested FOR-loops when calculating the values TDEV for all values of n, which is often required. With large values of N, which is typically the case, this results in a large calculation burden which either leads to long calculation times or to an increased amount of hardware for coping with the calculation burden in a reasonable amount of time. As an example, in communication systems using the above described TDEV as a control parameter for synchronization control, this leads to more circuitry, which makes the systems more complicated and more expensive.

20 The above mentioned problem is not restricted to systems calculating the deviation for a clock signal with respect to a reference clock signal over time, but will occur in any system based on the above principle of calculating a value representative of a variation based on the double sum

$$25 \quad \sum_j \left[\sum_{i=f_1(j)}^{f_2(j)} (X_{i+2n} - 2X_{i+n} + X_i) \right]^2 \quad (3),$$

where the lower and upper boundaries of the inner sum running over i are respective functions (f₁ and f₂) of the outer variable j.

30 [Object of the invention]

The present invention has the object of providing a better method of measuring a value characteristic of the variation between a quantity and a reference quantity, said value being based on the above described double sum.

5 [Summary of the invention]

This object is solved by the methods and devices described in the independent claims appended to the present application. Advantageous embodiments are described in the
10 dependent claims.

The present invention greatly simplifies the determination of a value representative of the variation between a quantity and a reference quantity by employing a recursive
15 formula, such that the two nested FOR-loops mentioned above can be avoided.

More specifically, the present invention defines a first value w_1 as a function of the difference values x_j , which
20 represent differences between the quantity and the reference quantity, and determines the value R , which corresponds to the above mentioned double sum, through

$$R = w_1^2 + \sum_{j=2}^{N-3n+1} w_j^2 \quad (6)$$

25

where each consecutive value of w_j is not calculated by running through a total sum, but is recursively determined from the respectively previous value w_{j-1} . n is a value between 1 and the integer part of $N/3$.

30

In this way the present invention achieves a simpler and less time consuming calculation of the value R , such that the measurement method of the present invention enables a simpler and cheaper hardware, without any decrease in
35 efficiency. More specifically, the calculation of the double sum of the above mentioned equation (3) requires

5 floating point operations in a number depending on N^2 ,
 whereas the method of the present invention only requires a
 number of floating point operations depending on N .

Therefore, the present invention decreases the required
 10 processing capacity and processing time, to thereby lead to
 better and/or cheaper hardware.

According to a preferred embodiment of the present
 invention, the calculation of w_1 is done in accordance with
 15

$$w_1 = \sum_{k=1}^n (x_{k+2n} - 2x_{k+n} + x_k),$$

and the recursive calculation of w_j in accordance with

$$w_j = w_{j-1} + x_{j-1+3n} - 3x_{j-1+2n} + 3x_{j-1+n} - x_{j-1}.$$

20

According to another preferred embodiment of the present
 invention, the calculation of w_1 is performed by
 introducing a help variable y , where

$$25 \quad y_k = x_{k+2n} - 2x_{k+n} + x_k \quad (8)$$

and

$$w_1 = \sum_{k=1}^n y_k \quad (9)$$

30

such that the recursive formula for w_j becomes

$$w_j = w_{j-1} + y_{j-1+n} - y_{j-1} \quad (10)$$

5

According to further preferred embodiments, the values R , which depend on n , can be used to calculate a variance and a deviation value, either for individual values of n , or for all values of n from 1 to the integer part of $N/3$.

10

As another preferred embodiment of the present invention, the measurement method is applied to a communication system requiring synchronization, in which the deviation value that is calculated relates to the variation between a clock
15 signal and a reference clock signal. According to another preferred embodiment, the present invention is applied to a system in which a surface profile level is compared to a reference profile level, and samples are measured at equal location intervals, such that the measured characteristic
20 variation value relates to the spatial variation of the surface level.

As already mentioned above, the present invention can be applied to a system calculating a value characteristic of a
25 variation on the basis of the above mentioned double sum shown in equation (3).

[Brief description of the figures]

30

Fig. 1a and 1b

show a flow-chart illustrating a first embodiment of the present invention;

Fig. 2a and 2b

show a flow-chart illustrating a second embodiment of the present invention;
and

35

Fig. 3a and 3b

show a flow-chart illustrating a fourth embodiment of the present invention.

5 Fig. 4 is a diagram illustrating the sampling number N , the measurement period $N\tau_0$, the sampling interval $n\tau_0$, and the basic interval τ_0 .

10 Fig. 5a and 5b show a flow-chart illustrating an embodiment that is a modification of the embodiment shown in Fig. 1.

15 Fig. 6a and 6b show a flow-chart illustrating a third embodiment of the present invention.

20 Fig. 7a and 7b show a flow-chart illustrating an embodiment of the present invention that is a modification of the embodiment shown in Fig. 6.

[Detailed disclosure]

25 Fig. 1 shows a flow-chart of a first embodiment of the present invention, where Fig. 1a shows the first part and Fig. 1b the second part. As can be seen, in a first step S1 a loop variable i is set to a starting value of 1. Then, in step S2, a quantity Q , which depends on a given parameter t is measured at equidistant intervals τ_0 , together with a
30 reference quantity Q_{ref} associated with Q , where Q_{ref} also depends on the parameter t . In this way, samples $Q_i = Q(i \cdot \tau_0)$ and $Q_{ref_i} = Q_{ref}(i \cdot \tau_0)$ are measured. Also, the difference between Q_i and Q_{ref_i} is determined to thereby supply error samples $x_i = Q_i - Q_{ref_i}$. It is self-understood
35 that the error function can also be defined as $Q_{ref_i} - Q_i$. It should be noted that t represents any possible

5 parameter, such as time, location, etc. The interval τ_0 is naturally measured in the same units as the parameter t .

Then, N samples are determined by running through the loop constituted by steps S2, S3 and S4, where step S3
10 determines if $i = N$, and if not, then S4 increments the loop variable i to $i + 1$. N is a parameter that characterizes the measurement period, as will be explained in more detail in connection with Fig. 4. With regard to the present invention, it is of no importance how N is set
15 or acquired, i.e. with respect to the invention, N can be seen as an arbitrary, given parameter.

It should be noted that the quantity Q can be any measurable quantity, just as the parameter t can be any
20 parameter on which a quantity can depend. As an example, Q can be a clock signal T and the parameter t can be the actual time, so that x would be the difference between a clock signal $T(t)$ and a reference clock signal $T_{ref}(t)$ at equal spacing sample points defined by the time interval
25 τ_0 . On the other hand, the quantity Q can equally well be a surface level value and the parameter referred to as t a one dimensional location along said surface, such that x represents error values between surface level values and reference surface level values at points of equal distance
30 τ_0 along a direction in said surface.

After the samples x_i are determined, a second loop using a loop variable k determines a value W_1 . More specifically, in step S5 the loop variable k is set to 1 and the value W_1
35 is set to 0. Then, a loop consisting of steps S6, S7 and S8 determines a value W_1 in accordance with the above mentioned equation (4) which is

5

$$W_1 = \sum_{k=1}^n (X_{k+2n} - 2X_{k+n} + X_k) \quad (4)$$

10 This is done by replacing the value W_1 by $W_1 + X_{k+2n} - 2X_{k+n} + X_k$ in step S6, then determining if $k = n$ in step S7 and incrementing k to $k+1$ in step S8 if the result in S7 is negative.

15 It should also be noted that the value for n is acquired in step S5. As will be explained in more detail in connection with Fig. 4, n is a parameter that characterizes the observation interval. With regard to the present invention, n can be acquired or set in any desirable or suitable way. For example, n can be a stored value that is simply read by the system in step S5. Or the user may be prompted to enter
20 a desired value. Or the system may have a sub-routine for determining a value of n . As can be seen, it is of no importance to the invention how and where n is set, as long as the value of n lies between 1 and the integer part of $N/3$.

25

Then, in step S81 it is determined if n is equal to the integer part of $N/3$, and if this is the case, then the value R , which represents the above mentioned double sum

$$30 \quad \sum_j \left[\sum_i (X_{i+2n} - 2X_{i+n} + X_i) \right]^2 \quad (3)$$

is determined as $R = W_1^2$. This is shown in step S9 (see Fig. 1b).

5 On the other hand, if in step S81 it is determined that n is smaller than the integer part of $N/3$, then the processing proceeds to step S10, in which again the above mentioned value of R is set to w_1^2 but then processing
 10 continues by setting the loop variable j to 2 in step S11 and then entering the loop as S12, S13, S14 and S15 to thereby determine the value R as

$$R = w_1^2 + \sum_{j=2}^{N-3n+1} w_j^2 \quad (6)$$

15 where each value w_j is determined recursively from the previous value of w , i.e. w_{j-1} by

$$w_j = w_{j-1} + x_{j-1+3n} - 3x_{j-1+2n} + 3x_{j-1+n} - x_{j-1} \quad (7)$$

20 This is done by calculating the new value of w_j in accordance with the above mentioned equation (7) in steps S12, then replacing the value of R by $R + w_j^2$ in step S13, asking if the value j has reached $N - 3n + 1$ in step S14 and
 25 incrementing j to $j+1$ in step S15 if the result of step S14 is negative.

The processing after step S14 or S9 runs together again, i.e. the value of R is then employed in any suitable way,
 30 e.g. output to a control means that responds to the measure of variation between Q and Q_{ref} expressed by R , or the value R is processed further, e.g. a variance value VAR is determined as

$$\text{VAR} = \frac{R}{6n^2(N-3n+1)} \quad (11)$$

and/or a deviation value is determined as $\text{DEV} = (\text{VAR})^{1/2}$ or

$$\text{DEV} = \sqrt{\frac{R}{6n^2(N-3n+1)}} \quad (12)$$

10

The above mentioned embodiment calculates one value representative of a variation between a quantity Q and a reference quantity Q_{ref} associated with Q in dependence on a parameter n , where n determines the observation interval in the form of $n \cdot \tau_0$. n can be assigned or have any value between 1 and the integer part of $N/3$, where N indicates the measurement period $N \cdot \tau_0$.

As can be seen, the above embodiment does not contain any nested loops, i.e. loops that are part of a larger outer loop. In this way, the above described double sum

$$\sum_j \left[\sum_{i=f_1(j)}^{f_2(j)} (x_{i+2n} - 2x_{i+n} + x_i) \right]^2 \quad (3)$$

is calculated only from single, independent loops, so that the amount of necessary calculation only depends linearly on the sample size, i.e. only depends on N , in contrast to a conventional solution of the double sum, which would lead to a number of calculations depending on N^2 . Therefore, the above described embodiment achieves a better measurement method, as the amount of calculation is considerably

5 reduced, namely by a factor of N, which in turn allows a far simpler and/or more efficient hardware implementation.

The present invention is by no means restricted to the specific embodiment described in Fig. 1a and 1b, as a
 10 person skilled in the art will readily see that the precise steps of calculation and looping can be arranged in any desired or suitable way. An example of this is shown in Figs. 2a and 2b which show a second embodiment of the present invention. Steps in Figs. 2a and 2b which are the
 15 same as those already described in Figs. 1a and 1b carry the same reference numerals and shall not be described again in detail.

Instead of one loop S2, S3 and S4 for measuring Q_i , Q_{ref_i}
 20 and determining x_i , as in the case of Fig. 1, Fig. 2 has two loops S20, S3, S4 and S22, S23, S24. In other words, the measurement of Q_i and Q_{ref_i} and the determination of x_i is performed in two subsequent loops. On the other hand, the value $R = w_1^2$ is not determined in steps S9 and S10, as
 25 in Fig. 1, but only in one step S25, which precedes the decision in step S8. Therefore, as already mentioned, the present invention can basically be implemented in any desired way, as long as the sum

$$30 \quad R = w_1^2 + \sum_{j=2}^{N-3n+1} w_j^2 \quad (6)$$

is determined in a recursive way by determining w_j from the preceding value w_{j-1} .

35 This is exemplified by a third embodiment of the present invention, a flow chart of which is shown in Fig. 6a and

5 6b. The third embodiment relates to a process that
determines a deviation value TDEV. In Fig. 6a, step S100
represents the determination of N values of x_i , similarly
to the above description of the first and second
embodiments. Then, in step S101, n is assigned a value
10 between 1 and the integer part of $N/3$ (referred to as
 $\text{Int}(N/3)$). In the first two embodiments n was a given value
with respect to the process for determining R, e.g. n was
set by an external control means. As indicated in the
present embodiment, the invention is by no means restricted
15 thereto, and n can also be set in the process for
determining R. It is clear that the setting of n is of no
importance to the basic concept of the invention, namely
the recursive determination of R, as n is only a parameter
in said recursive determination process.

20 In step S102 and the subsequent loop consisting of steps
S103 to S105, similarly to steps S5 to S8 in the previous
embodiments, a first value of w is determined in accordance
with

25

$$W = \sum_{k=1}^n (x_{k+2n} - 2x_{k+n} + x_k)$$

Then, in step S106, a value of R is determined with the
help of the above calculated value of w, namely $R=w^2$. If
30 the value of n is equal to $\text{Int}(N/3)$, then the calculation
of R is complete, as step S107 will then branch to step
S113 (see Fig. 6b) to calculate TDEV on the basis of the
shown equation. On the other hand, if n is smaller than
 $\text{Int}(N/3)$, then R will be calculated recursively in
35 accordance with

$$5 \quad R = w_1^2 + \sum_{j=2}^{N-3n+1} w_j^2 \quad (6)$$

and

$$w_j = w_{j-1} + x_{j-1+3n} - 3x_{j-1+2n} + 3x_{j-1+n} - x_{j-1} \quad (7)$$

10 in steps S108 to S112.

Finally, after R has been determined, TDEV is calculated in step S113 in accordance with the shown equation.

15 A difference between the first two embodiments and the third embodiment is that in the third embodiment no vectorisation of w is necessary.

Figs. 3a and 3b show a flow-chart of a fourth embodiment of the present invention. Steps that are the same as in Fig. 1 carry the same reference numerals and shall not be described again in detail. The first loop S2, S3 and S4, which is identical to the one shown in Fig. 1, determines error values x_i which characterize the variation between a quantity Q and a reference quantity Q_{ref} . The present embodiment is characterized by the definition of a help variable y_k , as shown in the loop consisting of steps S51, S52 and S53. As can be seen, in a first step S50, the loop variable k is set to 1, and then the help variable y_k is defined in accordance with

20

25

30

$$y_k = x_{k+2n} - 2x_{n+k} + x_k \quad (8)$$

for values of k from 1 to N-2n. In the presently described embodiment, this is achieved by determining in step S52 if k is equal to N-2n, and if not, then incrementing k to k+1

35

5 in step S53, after which the processing returns to step S51. These values of y_k are then stored.

After all of the values y_k for $k = 1$ to $N-2n$ have been determined and stored, the processing enters a further loop referred to as S55, S56, S57. In this loop, which again runs through a loop variable referred to as k , the value w_1 is determined in accordance with the equation (9)

$$w_1 = \sum_{k=1}^n y_k \quad (9)$$

15

At first, in step S54, the loop variable k is set to 1 and the value w_1 is set to 0. Then w_1 is replaced by $w_1 + y_k$ (Step S55) after which step S56 asks if $k=n$, and if not, then k is incremented to $k + 1$ in step S57, after which the processing returns to step S55.

As in the case of in Fig. 2, the processing in Fig. 3 then continues with step S25, in which R is set equal to w_1^2 , after which step S81 determines if n is equal to the integer part of $N/3$. If not, then the loop formed by steps S60, S13, S14 and S15 is entered, which is comparable to the loops S12, S13, S14 and S15 known from the embodiments described in connection with Fig. 1 and 2, only that step S12 has been replaced by S60, in which the recursive determination of w_j is accomplished in accordance with

$$w_j = w_{j-1} + y_{j-1+n} - y_{j-1} \quad (10)$$

Although the above described embodiment contains the additional loop S51, S52 and S53 for determining the help

5 variable y_k , the resulting calculation in the recursive
equation of step S60 is simplified, which can be
advantageous because it requires simpler hardware,
especially if the method of the present invention is
10 implemented in the form of circuitry containing adders,
subtractors, etc. On the other hand, if the invention is
implemented as software in an appropriate computing device,
e.g. a CPU, then the embodiment described in connection
with Fig. 1 is advantageous over that described in
connection with Fig. 3, because the method embodied by the
15 flow-chart of Fig. 1 contains one loop less than that of
Fig. 3.

As already mentioned in connection with Fig. 1, the value R
determined by the methods described in connection with Fig.
20 2 and 3 can also be further employed in any suitable and
desired way, e.g. output to a control means that is
controlled in accordance with the variation between Q and
Qref, or processed further, e.g. for calculating a variance

$$25 \quad \text{VAR} = \frac{R}{6n^2(N-3n+1)} \quad (11)$$

or a deviation

$$30 \quad \text{DEV} = \sqrt{\frac{R}{6n^2(N-3n+1)}} \quad (12)$$

The value R determined by the methods in accordance with
the above described embodiments is equal to the double sum

$$\sum_j \left[\sum_i (x_{i+2n} - 2x_{i+n} + x_i) \right]^2 \quad (3)$$

described in the introduction. As already mentioned, the value n , which can be assigned any value between 1 and the integer part of $N/3$ describes the number of sampling intervals within one observation interval. This is explained in connection with Fig. 4, in which a number N of sampling intervals along the direction of a parameter t (for example time) are shown, each interval having a length of τ_0 . In the specific example of Fig. 4, $N = 12$. The observation interval $n\tau_0$ relates to the triplets of values x associated with each sampling interval, i.e. x_{i+2n} , x_{i+n} , x_i .

According to a preferred embodiment, the method of the present invention is employed such that all values of R relating to individual values of n , i.e. for all values of n from 1 to the integer part of $N/3$ are calculated. These values can then be processed further, e.g. for calculating the deviation DEV according to

$$DEV = \sqrt{\frac{R}{6n^2(N-3n+1)}} \quad (12)$$

for each value of n from 1 to the integer part of $N/3$, in order to use these deviation values as appropriate characterization parameters.

Such a measurement of all of the possible values R can simply be accomplished by introducing a further loop, as

5 e.g. done in Fig. 5, which is a modification of the
embodiment shown in Fig. 1. All of the steps that are the
same as in Fig. 1 carry the same reference numerals and
shall not be described again. In addition to the steps of
Fig. 1, the embodiment for calculating the values for n
10 from 1 to the integer part of $N/3$ has the supplementary
step S70 between steps S3 and S5, in which the loop
parameter n is initially set to 1, and the supplementary
steps S71, S72 and S73, where the value R calculated for a
specific value n is stored in association with n in step
15 S71, and steps S72 and S73 for the outer loop running over
 n , where S72 asks if n has reached the maximum value which
is the integer part of $N/3$ and if not, then the processing
proceeds to steps S73, in which n is incremented to $n+1$.

20 After step S73, the loop returns to S5. As in the cases of
the previous embodiments, the values R can be processed or
output in any suitable or desired way.

It is clear that the embodiment described in connection
25 with Figs. 5a and 5b can also be realized in other ways,
for example also in connection with the embodiments
described in Fig. 2 and 3. The modification of the method
shown in Fig. 2 would consist in introducing the step S70
shown in Fig. 5a between steps S23 and S5 and Fig. 2a, and
30 adding steps S71, S72 and S73 at the end of the processing
in Fig. 2b, as done in Fig. 5b. Similarly, the method
described in connection with Fig. 3a would be modified by
adding step S70 between steps S52 and S54 of Fig. 3a and
adding steps S71, S72 and S73 at the end of the processing
35 in Fig. 3b. This is readily understandable to a person
skilled in the art.

Fig. 7a and 7b show a modification of the embodiment of
Fig. 6, where steps S201, S202 and S203 have been added in

5 order to implement a calculation of $TDEV(n, \tau_0)$ for all values of n from 1 to the integer part of $N/3$. As can be seen, the loop for n is initialized in step S201 and loops back in step S202, and step S107 exits the loop when n is equal to the integer part of $N/3$.

10

As already mentioned in connection with the embodiment of Fig. 1, the precise order and implementation of calculations and loopings in the embodiments of Figs. 2, 3, 5, 6 and 7 is not important to the invention as long as the value R is calculated by recursively determining w in accordance with

15

$w_j = w_j(w_{j-1})$, i.e. from the previous value of w , and as a function of the difference values x , e.g. either by

$$20 \quad w_j = w_{j-1} + x_{j-1+3n} - 3x_{j-1+2n} + 3x_{j-1+n} - x_{j-1} \quad (7)$$

or by

$$w_j = w_{j-1} + Y_{j-1+n} - Y_{j-1} \quad (10).$$

25

As can be seen in the embodiment of Fig. 5, the calculation of the values R for all values of n leads to one nested loop, in contrast to the conventional calculation which contains two nested loops, namely one for the inner sum

30

$$\sum_j \left[\sum_i (X_{i+2n} - 2X_{i+n} + X_i) \right]^2 \quad (3)$$

and a second one for the outer loop running over n . Again, the number of calculations is reduced by a factor of N in the present invention, as the number of required

35

5 calculations in accordance with the embodiment shown in Fig. 5 is in the order of N^2 whereas the conventional calculation is in the order of N^3 .

As a best mode of putting the invention to practice, the
 10 inventor presently considers the method described in connection with Fig. 7a and 7b, where the quantity Q is a clock signal T , Q_{ref} is a reference clock signal T_{ref} , such that the values x_i are time error samples. The values R are calculated for all possible values of n , i.e. from $n = 1$ to
 15 $n =$ the integer part of $N/3$, such that a complete set of values of the time deviation

$$TDEV(n\tau_0) = \sqrt{\frac{1}{6n^2} \frac{1}{(N-3n+1)} \sum_{j=1}^{N-3n+1} \left[\sum_{i=j}^{n+j-1} (x_{1+2n} - 2x_{i+n} + x_i) \right]^2} \quad (2)$$

20 can be calculated from the values R through

$$DEV = \sqrt{\frac{R}{6n^2(N-3n+1)}} \quad (12)$$

for all possible values of n . These values $TDEV(n\tau_0)$ can
 25 then be used for characterization or supervision of reference timing signals.

The precise implementation of the present invention in terms of hardware or software can be done in any suitable
 30 or desired way. For example, if a used software language has a provision such that if the running variable of a FOR-loop is outside of the range given by the upper and lower values of the FOR-loop, said FOR-loop is not entered, then

5 e.g. the decision step S81 and loop consisting of S11, S14
and S15 in Fig. 2b can be implemented by such a FOR-loop
running from $k=2$ to $N-3n+1$. In other words, the decision
step S81 would be implicitly contained in the above
mentioned FOR-loop.

10

Although the present invention has been described in terms
of specific embodiments, it is by no means restricted
thereto. Much rather, the scope of the invention is defined
by the appended claims. Reference symbols in the claims
15 serve the purpose of better understanding and do not
restrict the scope.

5 [Claims]

1. Method for measuring a value that characterizes a variation between a quantity (Q) and a reference quantity (Qref) associated with said quantity, both
10 depending on a predetermined parameter (t), comprising:
- measuring N samples (Q_i , Q_{ref_i}) of said quantity (Q) and said reference quantity (Qref) at equally spaced
15 intervals (τ_0) of said parameter (t), N being an integer with $N \geq 3$,
 - calculating and storing N difference values x_i between each sample of said quantity (Q_i) and each
20 sample of said reference quantity (Q_{ref_i}) at each of said N sample points, the index i being an integer running from 1 to N,
 - calculating a value w_1 as a function of said
25 difference values x_i ,
 - calculating a value R representative of the variation between said quantity and said reference quantity as

30

$$R = w_1^2 + \sum_{j=2}^{N-3n+1} w_j^2,$$

where n is an integer from the set of 1 to the integer part of $N/3$, and each value w_j with $j > 1$ is calculated
35 recursively from the previous value w_{j-1} and as a

5 function of said difference values x_i , if n is smaller than the integer part of $N/3$, and

- calculating said value R as $R = w_1^2$ if n is equal to the integer part of $N/3$.

10

2. Method according to claim 1, characterized by

- calculating said value w_1 according to the equation

15

$$w_1 = \sum_{k=1}^n (x_{k+2n} - 2x_{k+n} + x_k),$$

and

20 - calculating said each value w_j with $j > 1$ from the previous value w_{j-1} in accordance with

$$w_j = w_{j-1} + x_{j-1+3n} - 3x_{j-1+2n} + 3x_{j-1+n} - x_{j-1}.$$

25 3. Method according to claim 1, characterized by

- calculating and storing values y_k defined as

$$y_k = x_{k+2n} - 2x_{n+k} + x_k,$$

30

for $k = 1$ to $N-2n$,

- calculating said value w_1 according to the equation

5
$$w_1 = \sum_{k=1}^n y_k, \text{ and}$$

- calculating said each value w_j with $j > 1$ from the previous value w_{j-1} in accordance with

10
$$w_j = w_{j-1} + y_{j-1+n} - y_{j-1}.$$

4. The method of one of claims 1 to 3, characterized in that a variance value VAR is calculated as

15
$$\text{VAR} = \frac{R}{6n^2(N-3n+1)}.$$

5. The method of claim 4, characterized in that said variance value is calculated for each value of n from 1 to the integer part of $N/3$.

20

6. The method of one of claims 1 to 3, characterized in that a deviation value DEV is calculated as

$$DEV = \sqrt{\frac{R}{6n^2(N-3n+1)}}.$$

25

7. The method of claim 6, characterized in that said deviation value is calculated for each value of n from 1 to the integer part of $N/3$.

- 30 8. The method of one of claims 1 to 7, characterized in that said parameter on which said quantity and said reference quantity depend is time.

- 5
9. The method of claim 8, characterized in that said quantity is a timing signal and said reference quantity is a reference timing signal.
- 10 10. The method of one of claims 1 to 7, characterized in that said parameter on which said quantity and said reference quantity depend is location.
- 15 11. The method of claim 10, characterized in that said quantity is a surface profile level and said reference quantity is a reference profile level.
- 20 12. A device for measuring a value that characterizes a variation between a quantity (Q) and a reference quantity (Qref) associated with said quantity, both depending on a predetermined parameter (t), comprising:
- 25 - a measuring means for measuring N samples (Q_i , Q_{ref_i}) of said quantity (Q) and said reference quantity (Qref) at equally spaced intervals (τ_0) of said parameter (t), N being an integer with $N \geq 3$,
- 30 - a calculating and storing means for calculating and storing N difference values x_i between each sample of said quantity (Q_i) and each sample of said reference quantity (Q_{ref_i}) at each of said N sample points, the index i being an integer running from 1 to N,
- 35 - a calculating means for calculating a value w_1 as a function of said difference values x_i , for calculating

5 a value R representative of the variation between said quantity and said reference quantity as

$$R = w_1^2 + \sum_{j=2}^{N-3n+1} w_j^2,$$

10 where n is an integer from the set of 1 to the integer part of N/3, and each value w_j with $j > 1$ is calculated recursively from the previous value w_{j-1} and as a function of said difference values x_i , if n is smaller than the integer part of N/3, and for calculating said
 15 value R as $R = w_1^2$ if n is equal to the integer part of N/3.

13. Device according to claim 12, characterized by said
 20 calculating means calculating said value w_1 according to the equation

$$w_1 = \sum_{k=1}^n (x_{k+2n} - 2x_{k+n} + x_k),$$

25 and calculating said each value w_j with $j > 1$ from the previous value w_{j-1} in accordance with

$$w_j = w_{j-1} + x_{j-1+3n} - 3x_{j-1+2n} + 3x_{j-1+n} - x_{j-1}.$$

30 14. Device according to claim 12, characterized by said calculating means calculating and storing values y_k defined as

5

$$y_k = x_{k+2n} - 2x_{n+k} + x_k,$$

for $k=1$ to $N-2n$, calculating said value w_1 according to the equation

10

$$w_1 = \sum_{k=1}^n y_k, \text{ and}$$

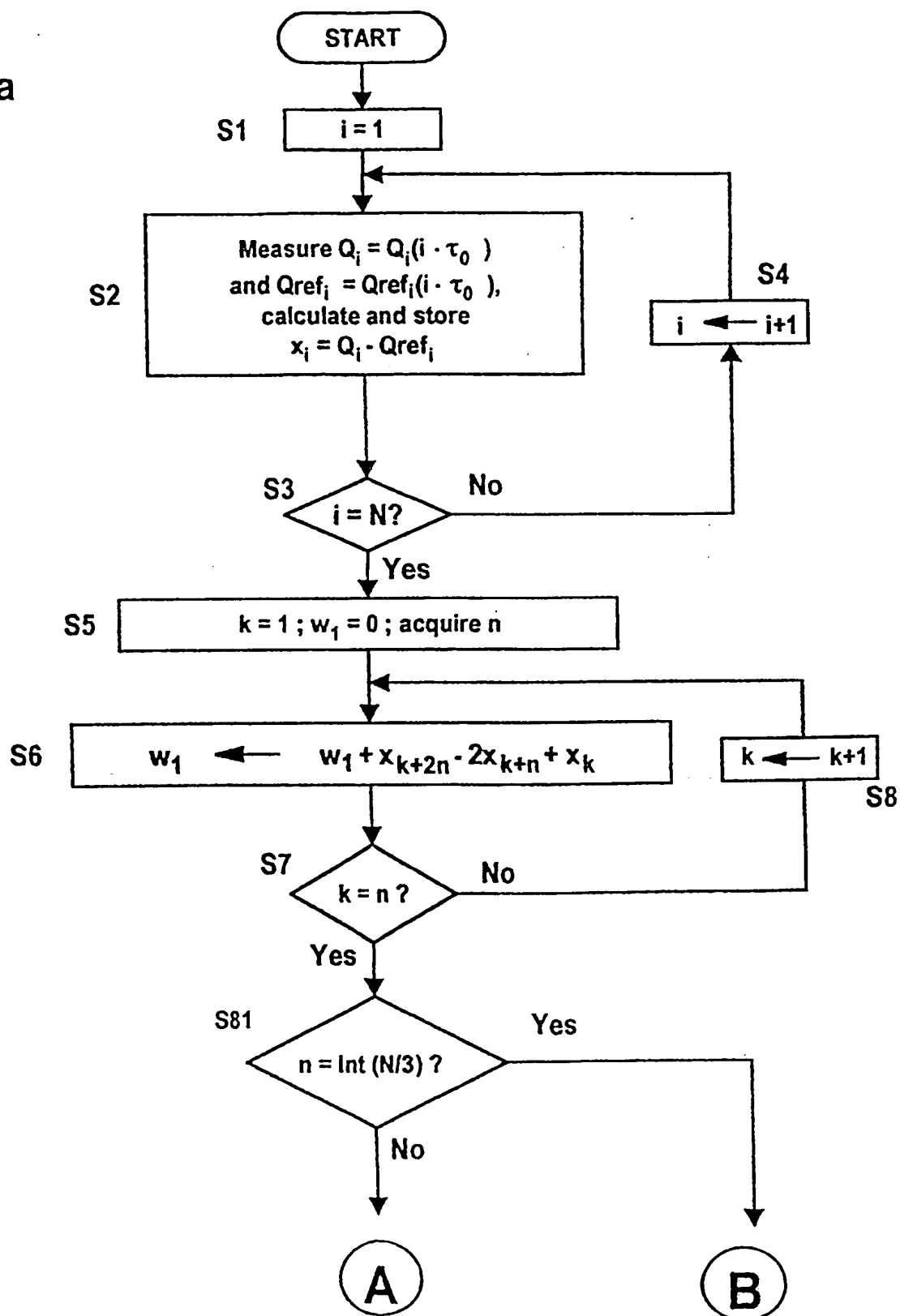
calculating said each value w_j with $j>1$ from the previous value w_{j-1} in accordance with

15

$$w_j = w_{j-1} + y_{j-1+n} - y_{j-1}.$$

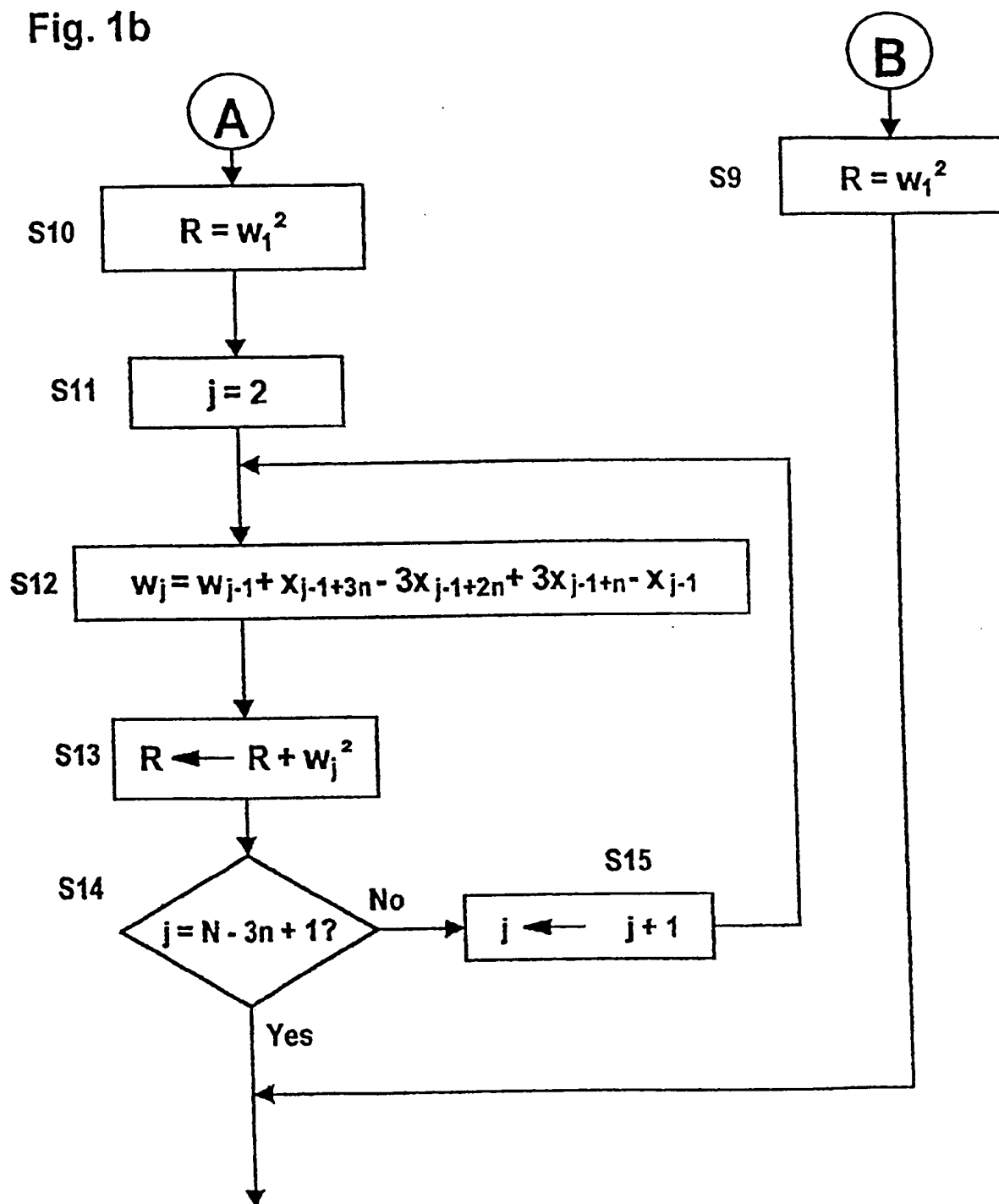
1/13

Fig. 1a



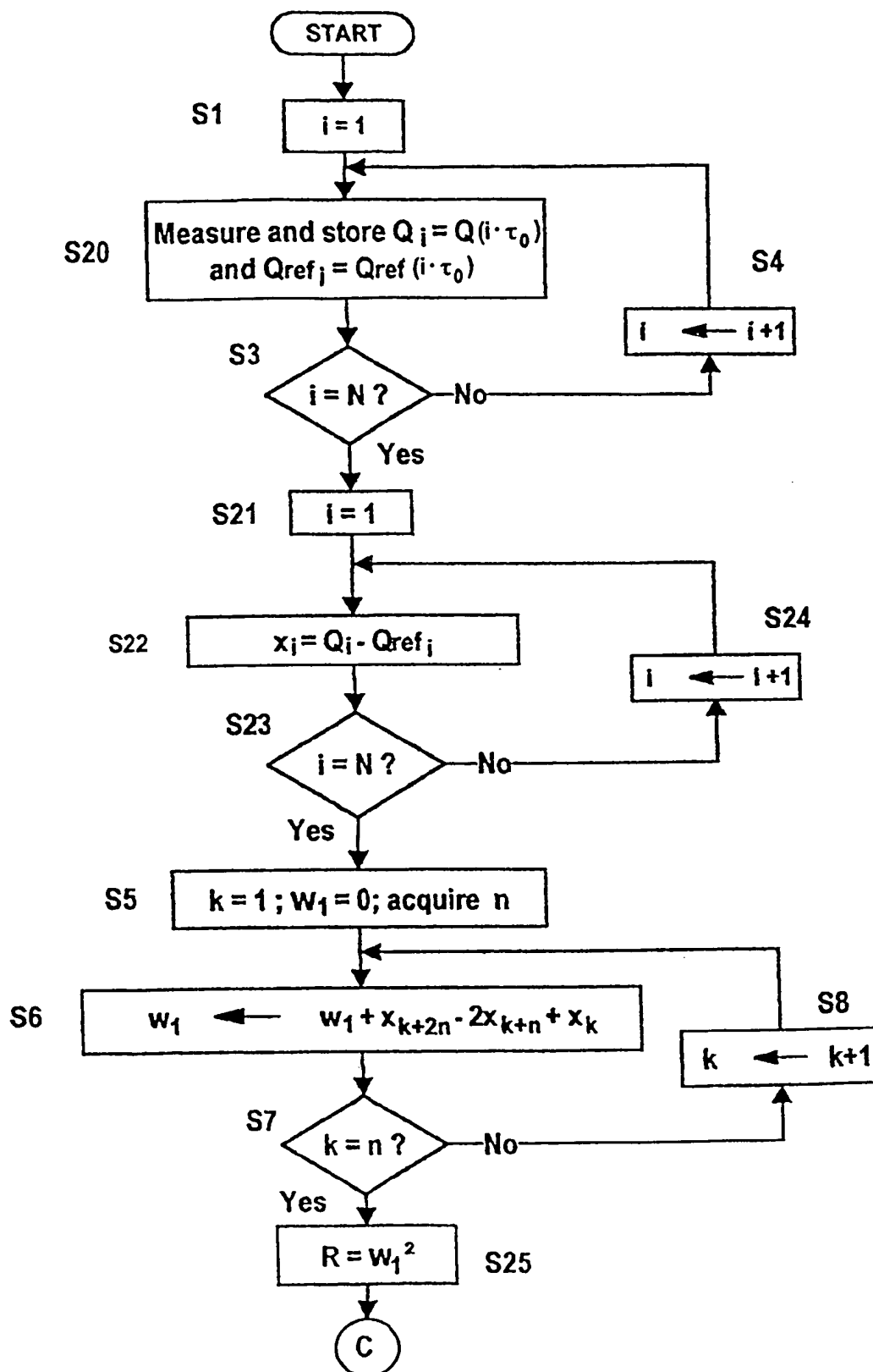
2/13

Fig. 1b



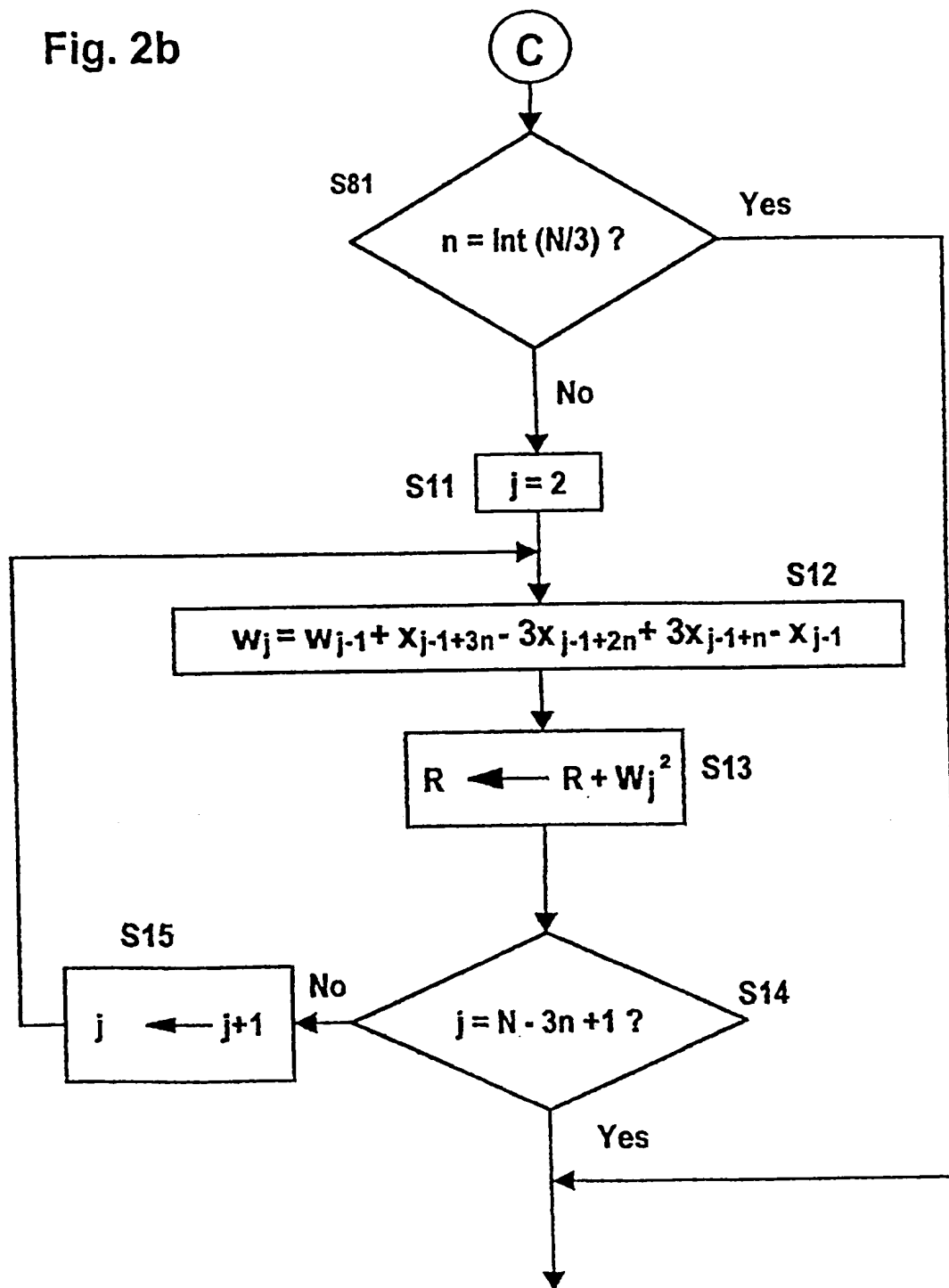
3/13

Fig. 2a



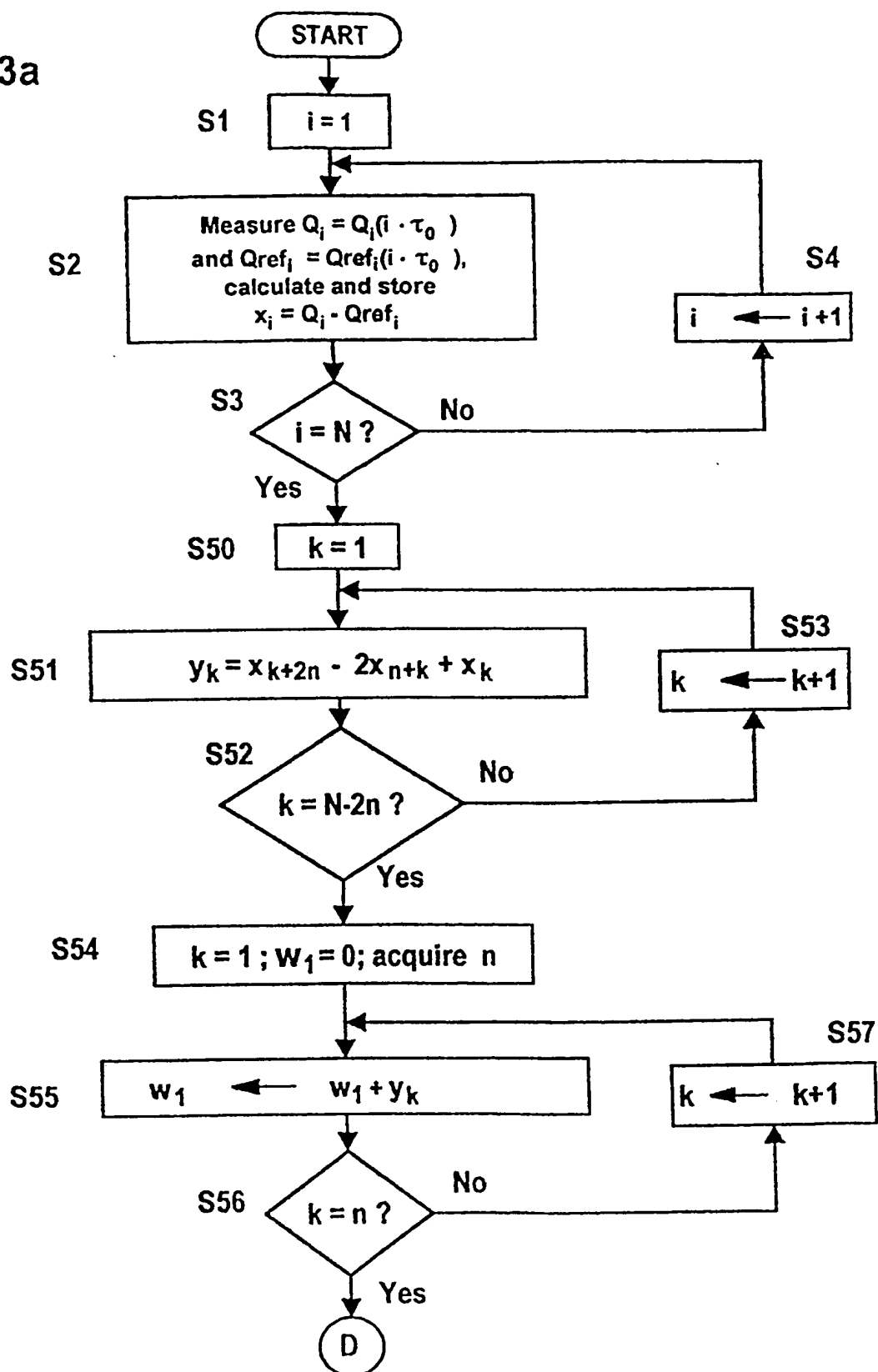
4/13

Fig. 2b



5/13

Fig. 3a



6/13

Fig. 3b

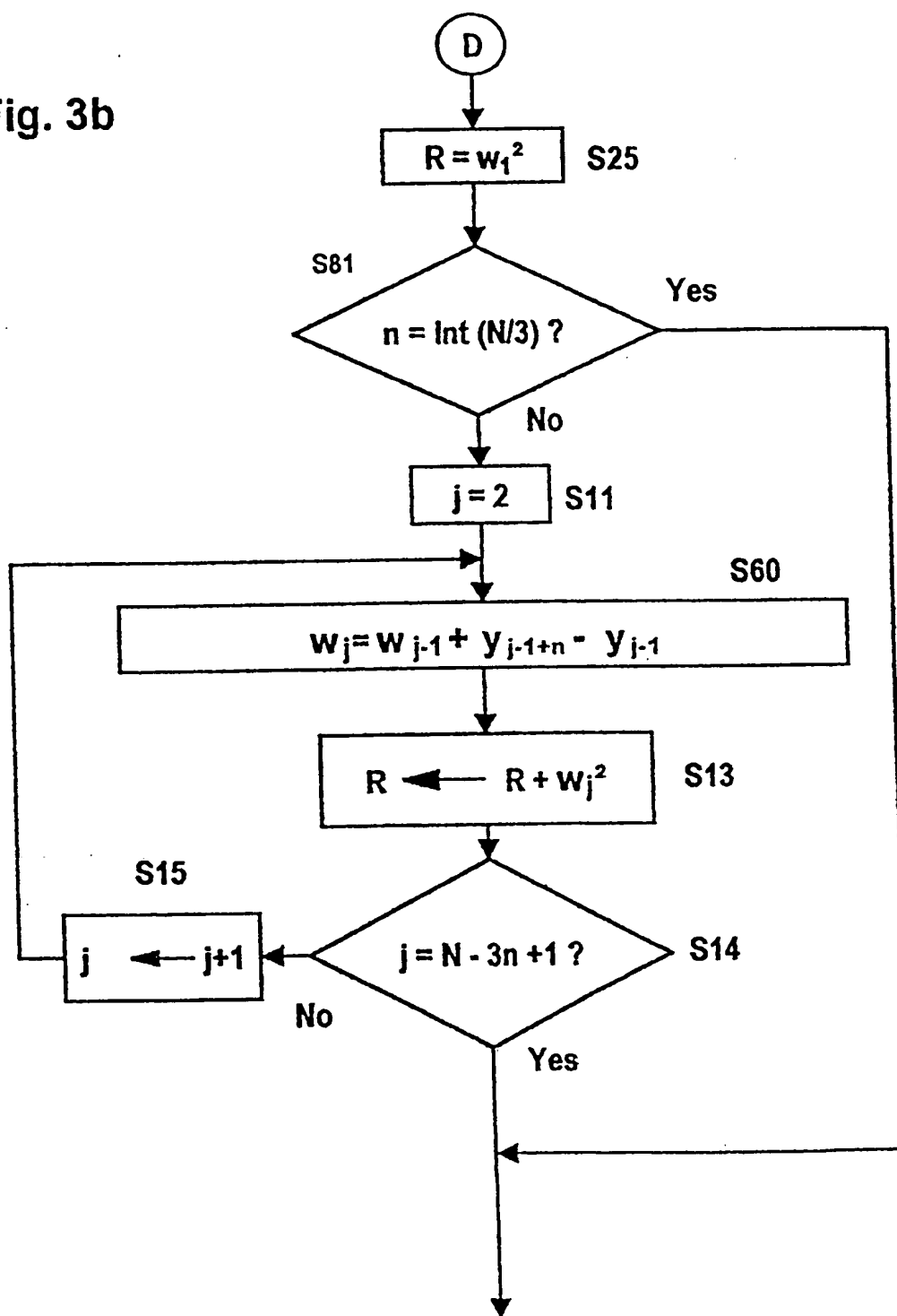


Fig. 4

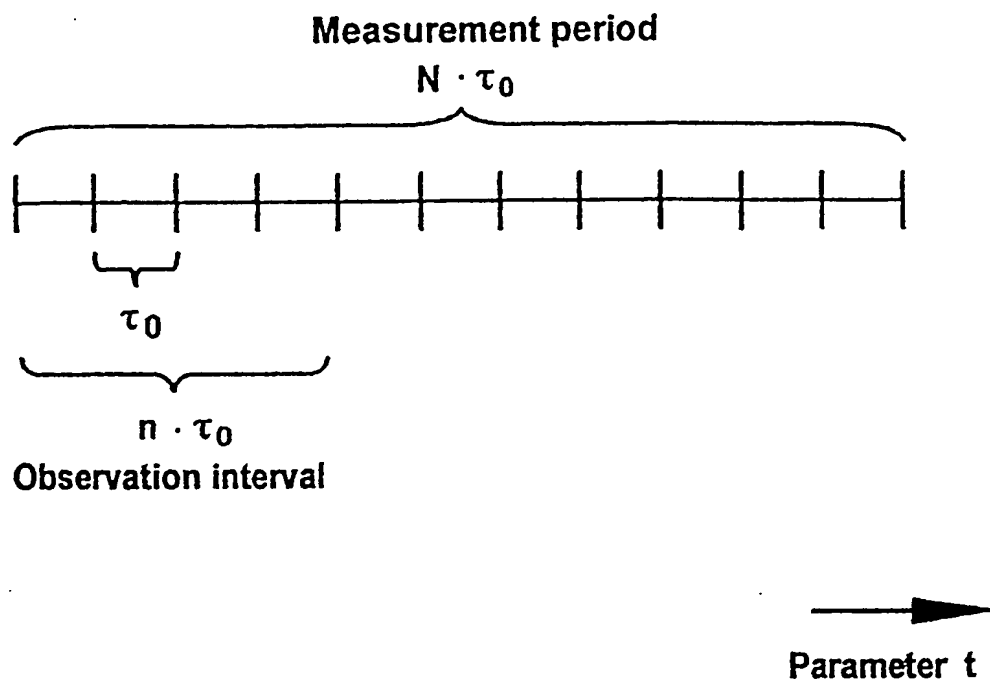
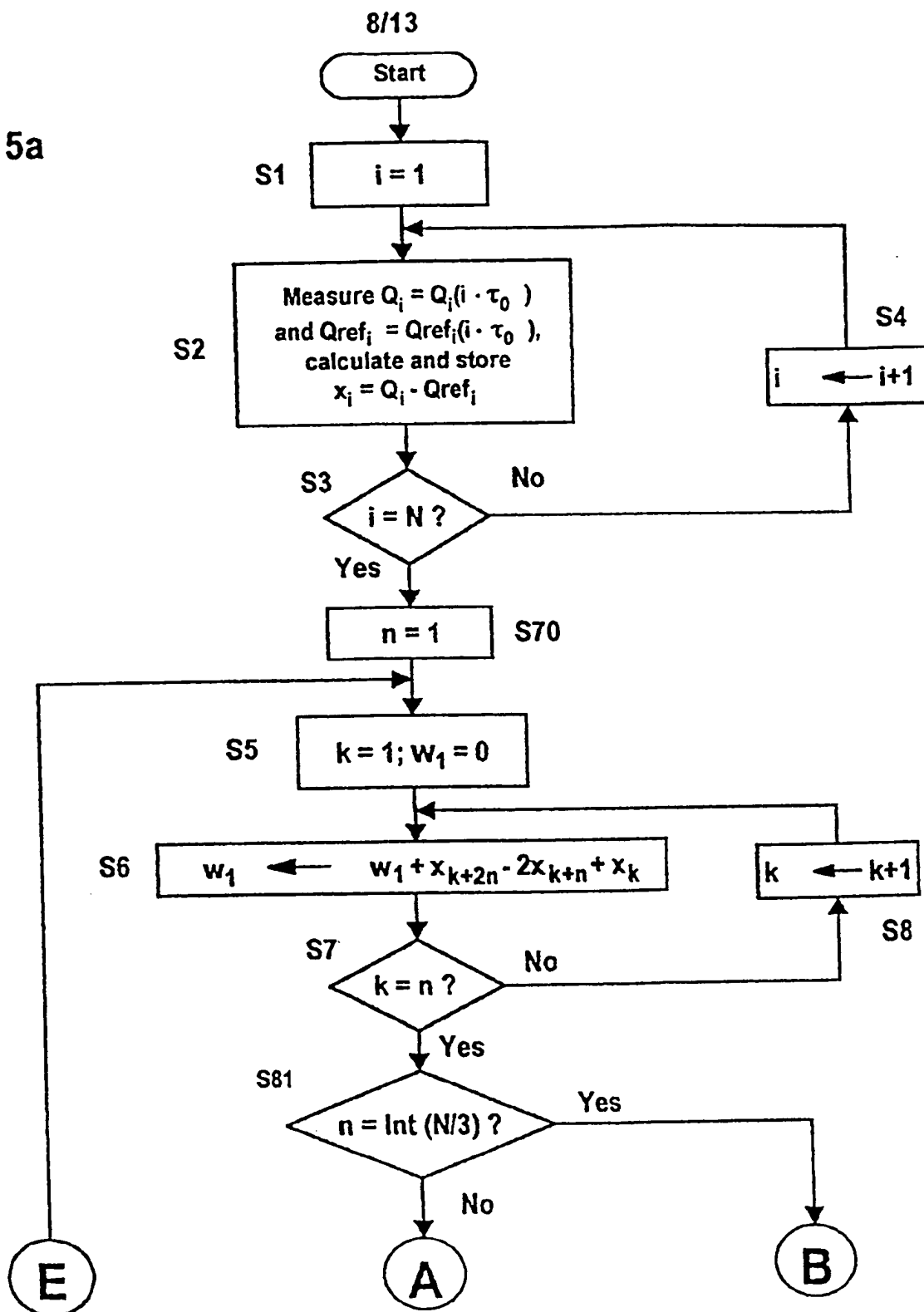


Fig. 5a



9/13

Fig. 5b

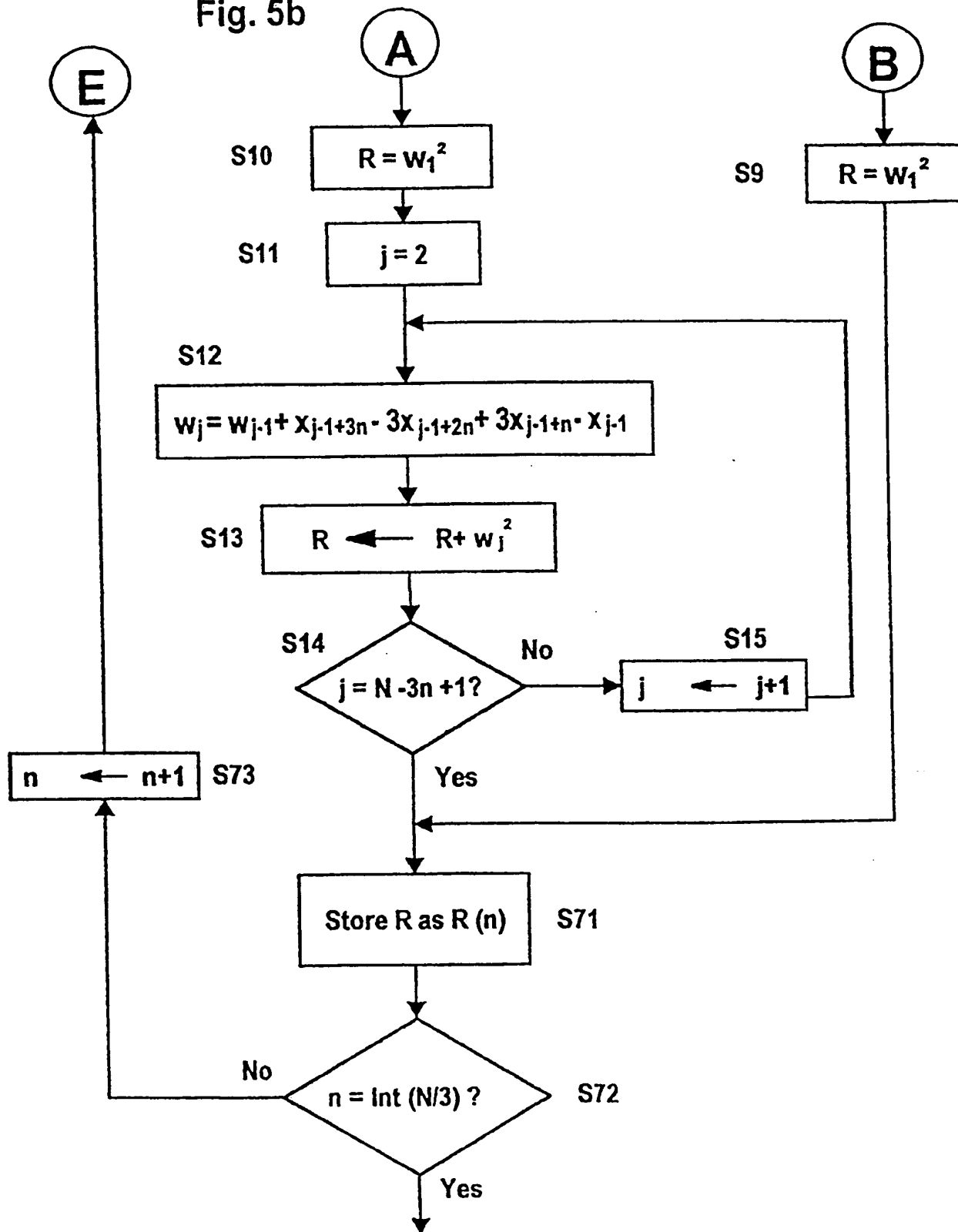
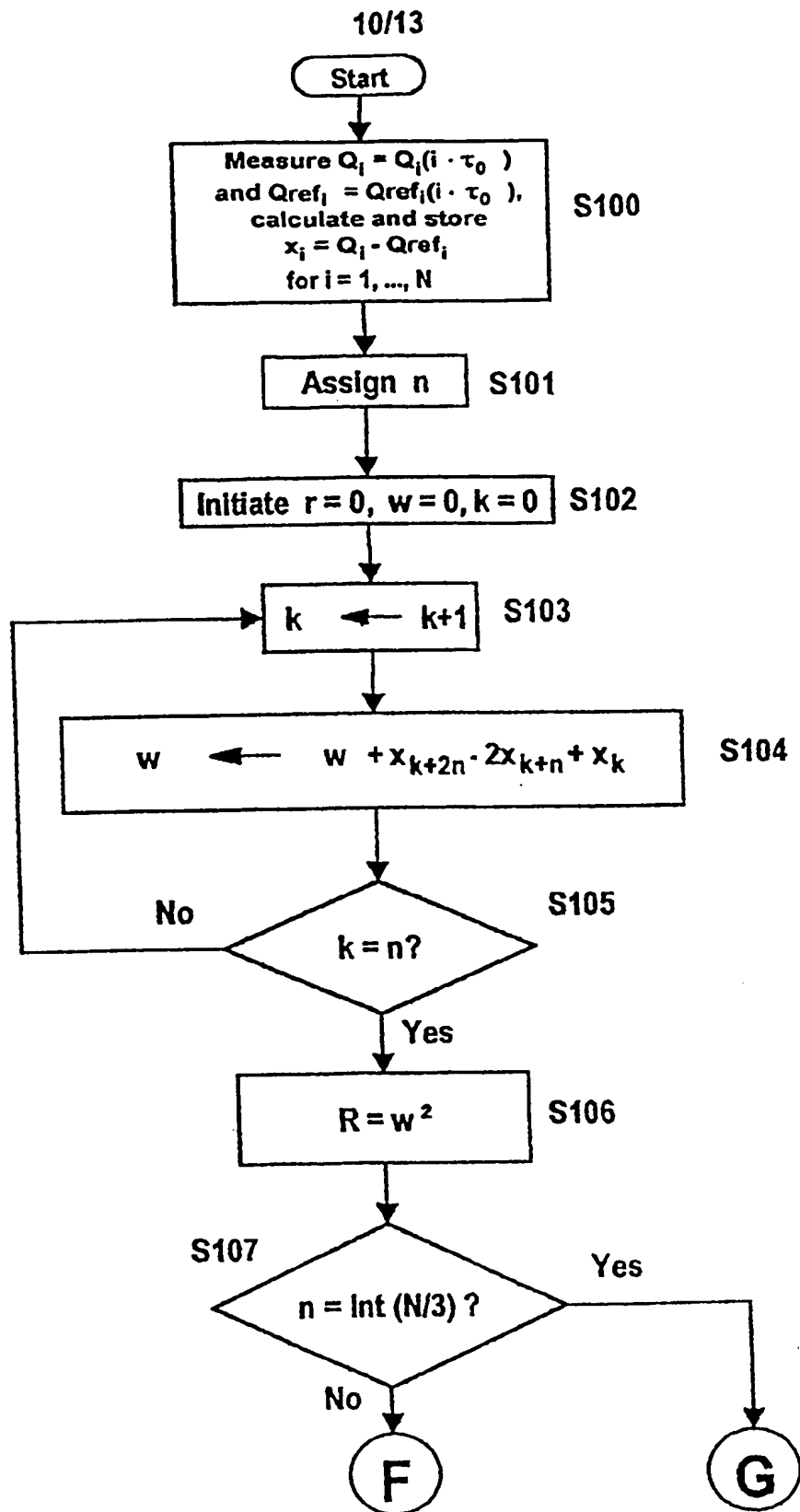
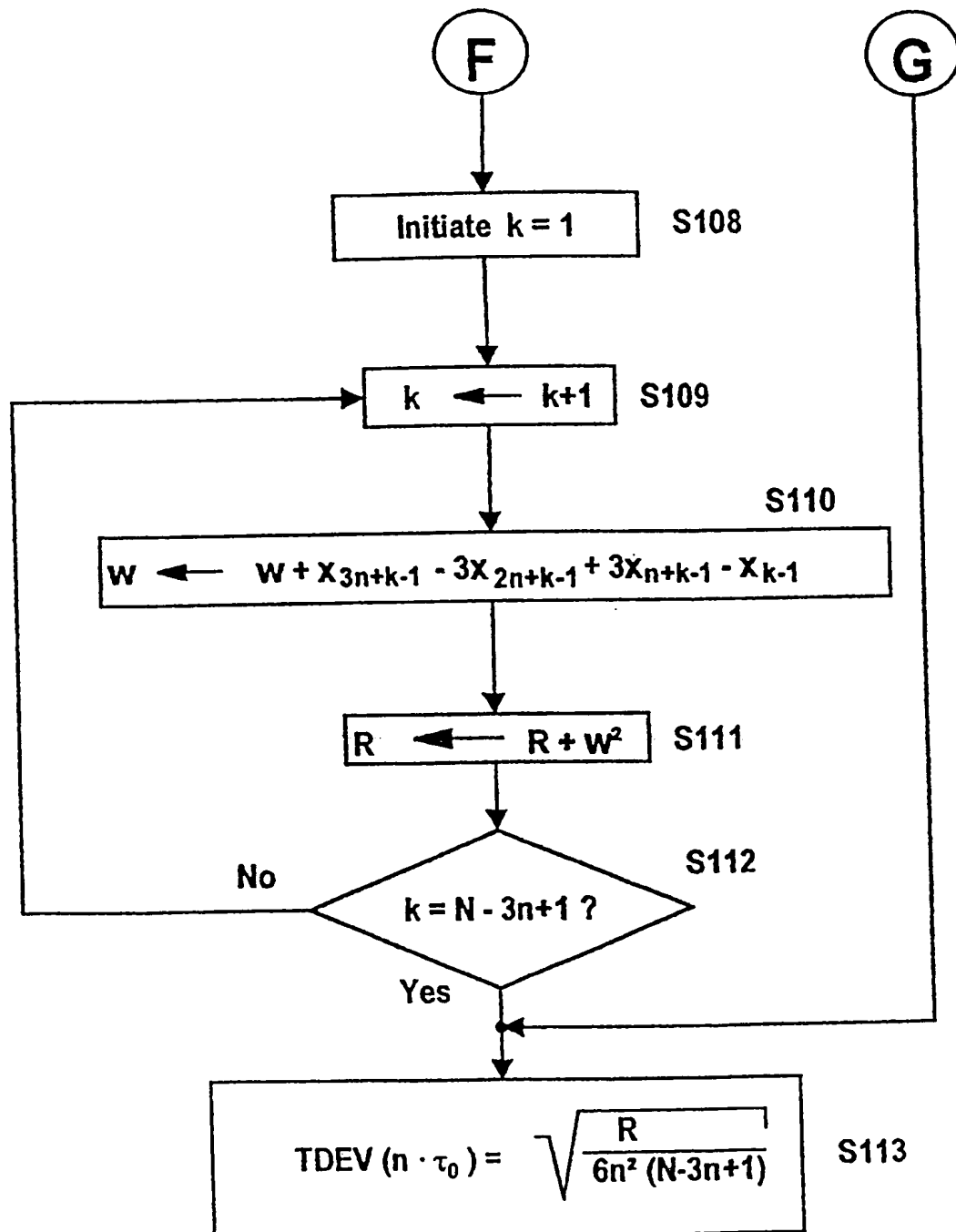


Fig. 6a



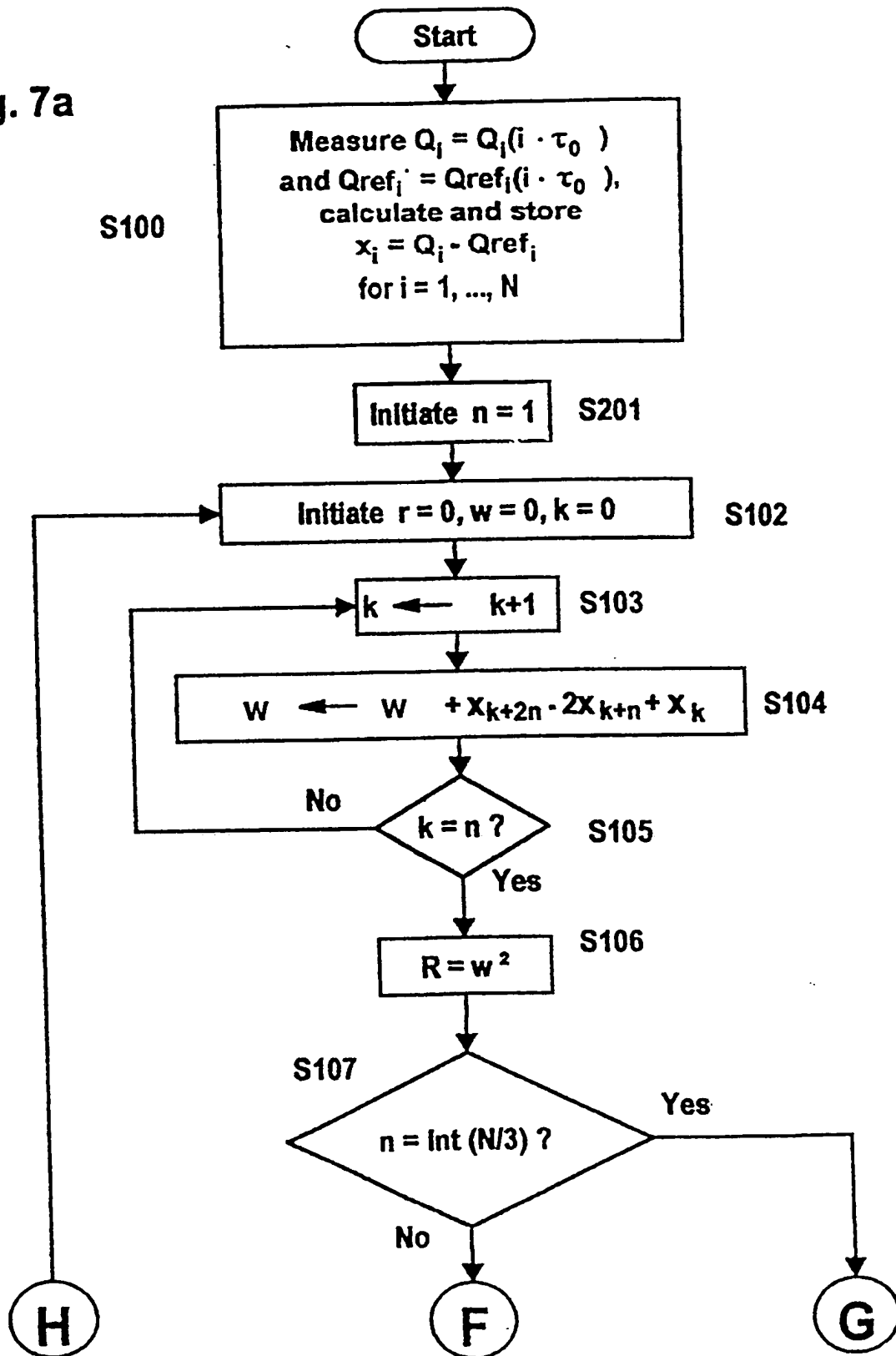
11/13

Fig. 6b



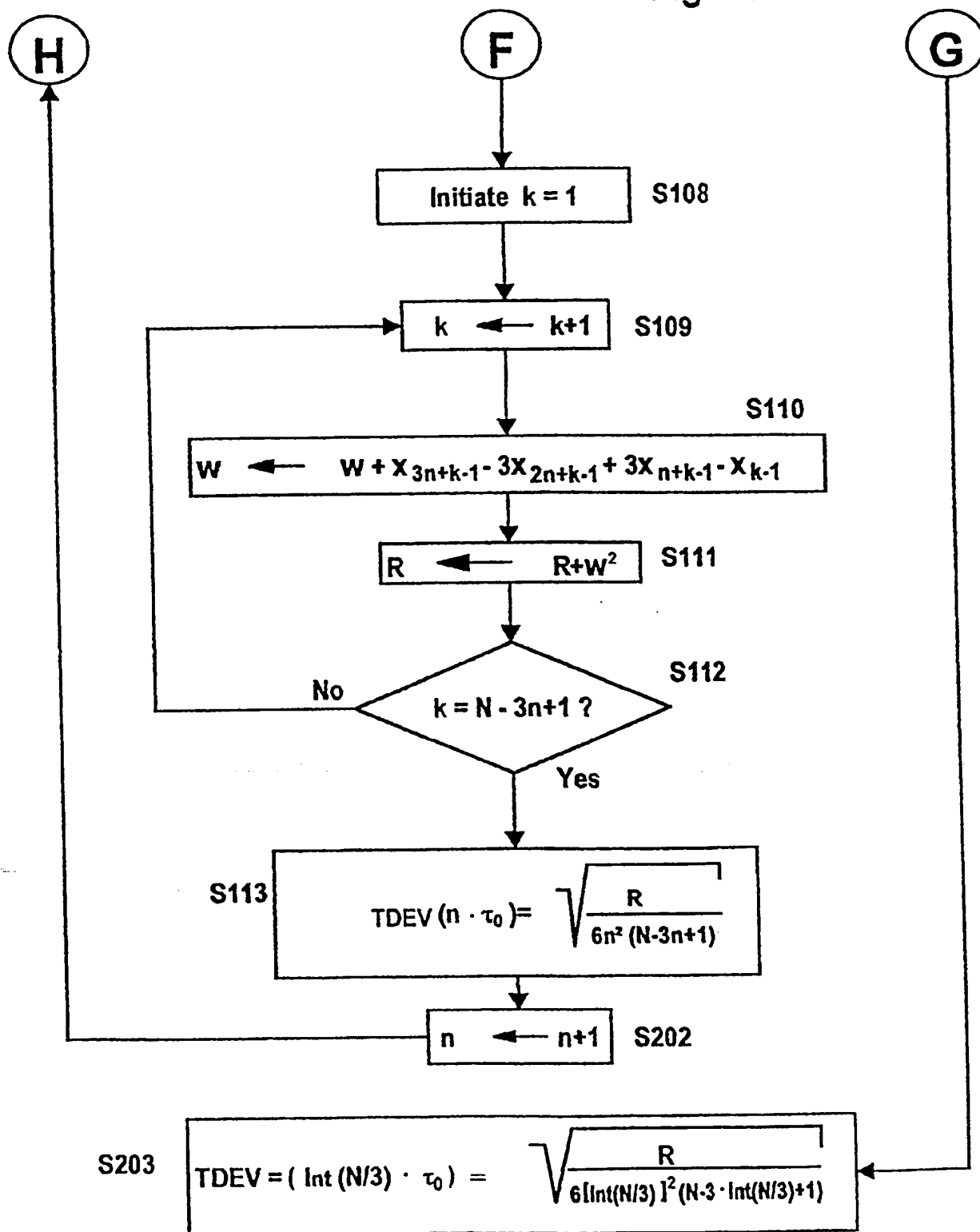
12/13

Fig. 7a



13/13

Fig. 7b



INTERNATIONAL SEARCH REPORT

Intern: 7al Application No

PCT/EP 99/03854

A. CLASSIFICATION OF SUBJECT MATTER
IPC 6 G06F17/18

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)
IPC 6 G06F

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practical, search terms used)

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category *	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
X	EP 0 055 156 A (THOMSON CSF) 30 June 1982 (1982-06-30) page 3, line 21 - line 26: claim 1 ---	1-14
A	EP 0 750 203 A (WESTERN ATLAS INT INC) 27 December 1996 (1996-12-27) claim 1 ---	1-14
A	G. DAHLQUIST, A. BJÖRCK: "Numerical Methods" 1974, PRENTICE-HALL, ENGLEWOOD CLIFFS, N.J. XP002116162 page 14, left-hand column, paragraph 1.3.2 -----	1-14

☐ Further documents are listed in the continuation of box C.☒ Patent family members are listed in annex.

* Special categories of cited documents:

- "A" document defining the general state of the art which is not considered to be of particular relevance
- "E" earlier document but published on or after the international filing date
- "L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)
- "O" document referring to an oral disclosure, use, exhibition or other means
- "P" document published prior to the international filing date but later than the priority date claimed

"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone

"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art.

"&" document member of the same patent family

Date of the actual completion of the international search

22 September 1999

Date of mailing of the international search report

06/10/1999

Name and mailing address of the ISA

European Patent Office, P.B. 5818 Patentlaan 2
NL - 2280 HV Rijswijk
Tel. (+31-70) 340-2040, Tx. 31 651 epo nl,
Fax: (+31-70) 340-3016

Authorized officer

Pierfederici, A

INTERNATIONAL SEARCH REPORT

Information on patent family members

International Application No

PCT/EP 99/03854

Patent document cited in search report		Publication date	Patent family member(s)		Publication date
EP 0055156	A	30-06-1982	FR	2496297 A	18-06-1982
			CA	1180124 A	25-12-1984
			US	4453223 A	05-06-1984
<hr/>					
EP 0750203	A	27-12-1996	US	5539704 A	23-07-1996
			CA	2178978 A	24-12-1996
			NO	962613 A	27-12-1996
<hr/>					